## Exercise 32

Tabular representations for the functions $f, g$, and $h$ are given below. Write $g(x)$ and $h(x)$ as transformations of $f(x)$.

| $x$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | -1 | -3 | 4 | 2 | 1 |
| $x$ | -3 | -2 | -1 | 0 | 1 |
| $g(x)$ | -1 | -3 | 4 | 2 | 1 |
| $x$ | -2 | -1 | 0 | 1 | 2 |
| $h(x)$ | -2 | -4 | 3 | 1 | 0 |

## Solution

$g(x)$ has the same outputs as $f(x)$ but with inputs off by 1.

$$
g(x)=f(x+1)
$$

$h(x)$ has the same inputs as $f(x)$ but with outputs off by 1.

$$
h(x)=f(x)-1
$$

